

IMPROVING BATTERY MODELS USING UNCERTAINTY ANALYSIS

Estimating experimental error and investigating propagation in models.



Siddhi Barhanpurkar, Edmund J. F. Dickinson

1. ABSTRACT

Battery models are increasingly desirable for automotive companies, motorsport and cell manufacturers to **design control systems** based on a particular cell. Models are as reliable as their **input parameters**, which are obtained from **physical measurements** made by tearing down a cell. Quantifying the uncertainty in these measurements and **propagating through the model** has a threefold impact:

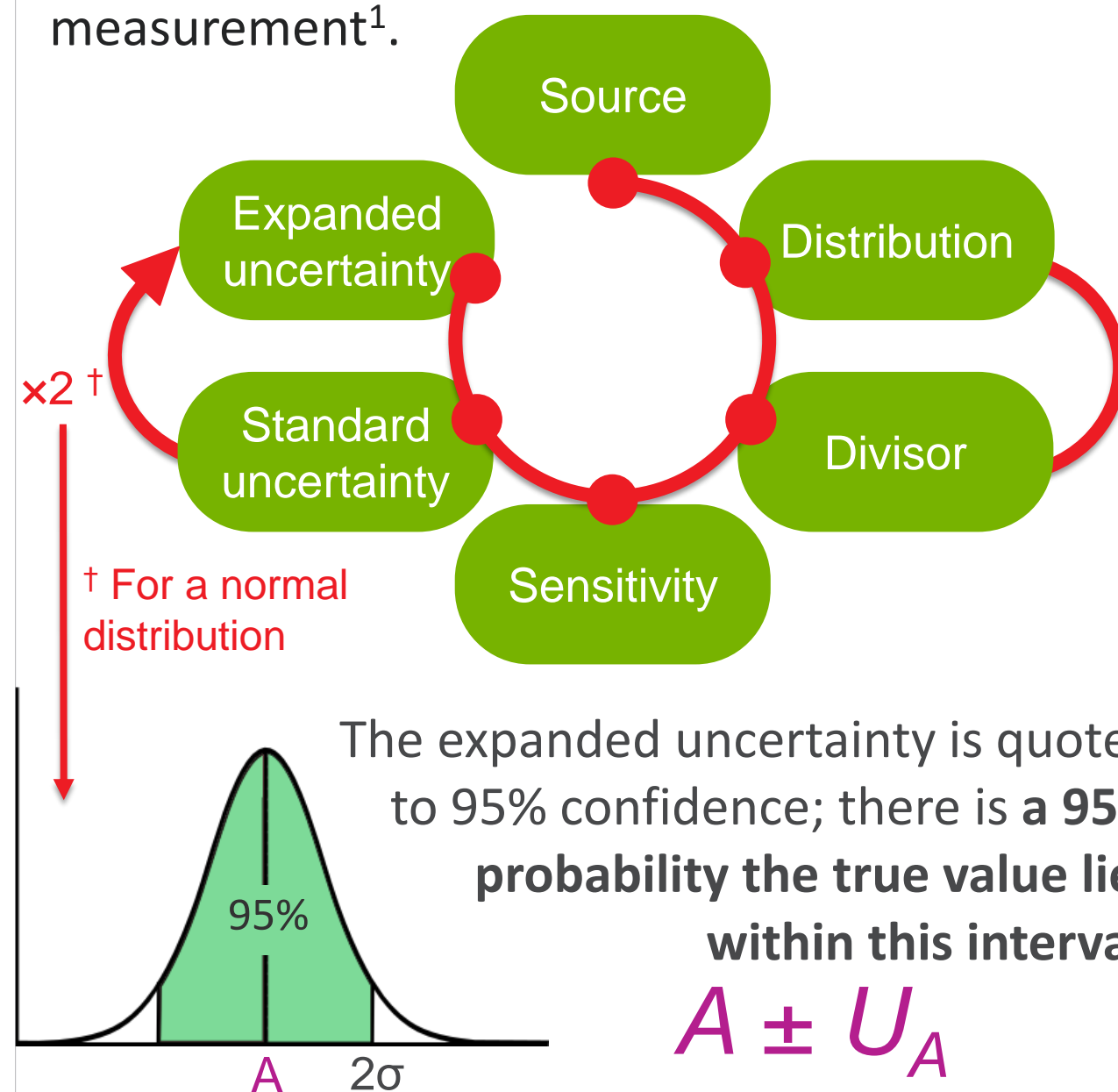
- 1) The reported data is more **trustworthy** for the customer.
- 2) The level of uncertainty may **affect decisions** such as amount of billing materials or manufacturing route used.
- 3) The sources of **uncertainty in the measurement method** are identified and the method can be improved.

Follow along with my website! Look for the magnifying glass symbol on the poster.

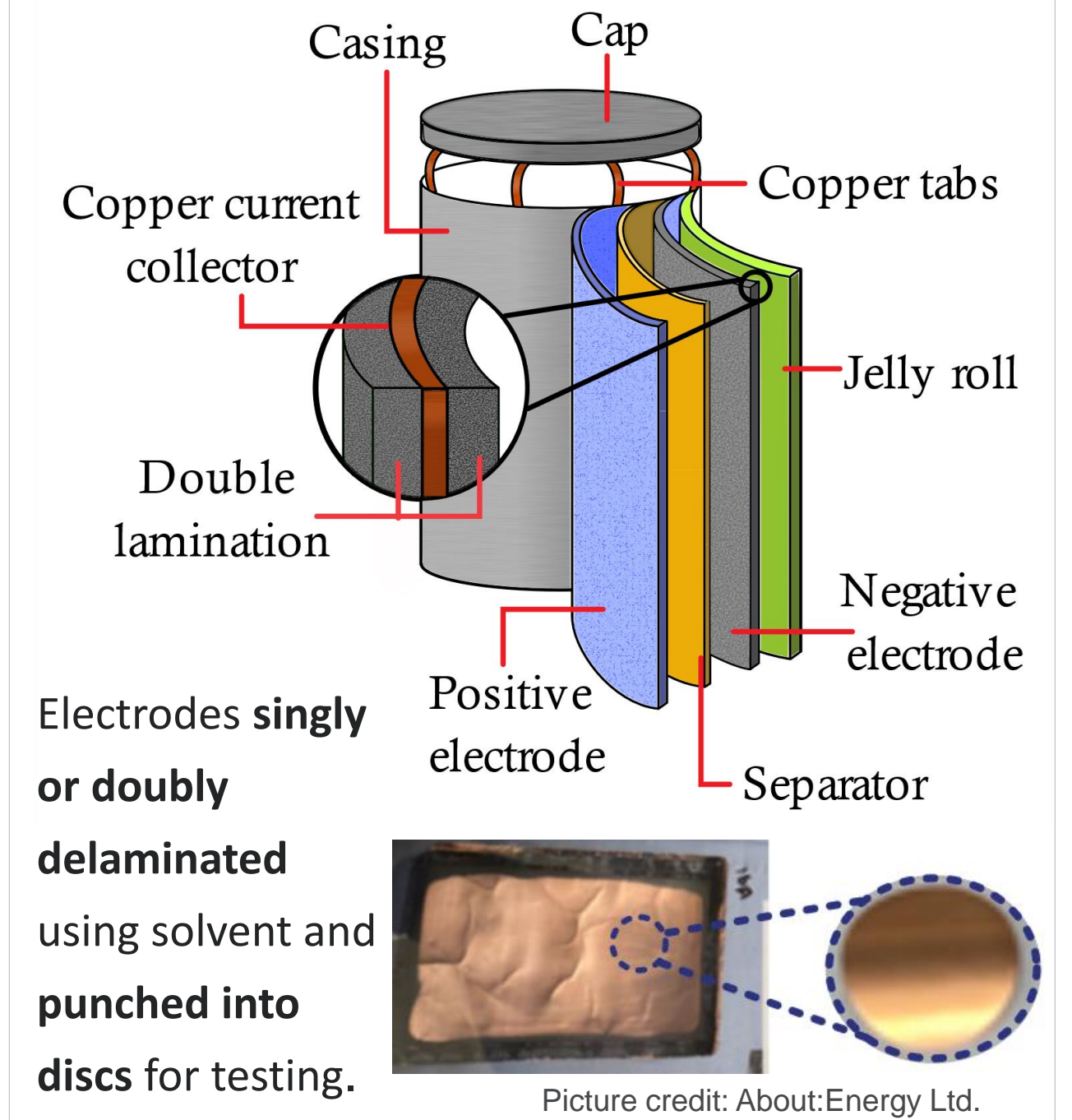


2. UNCERTAINTY BUDGETING

Uncertainty is the **quantification of doubt** in a measurement¹.

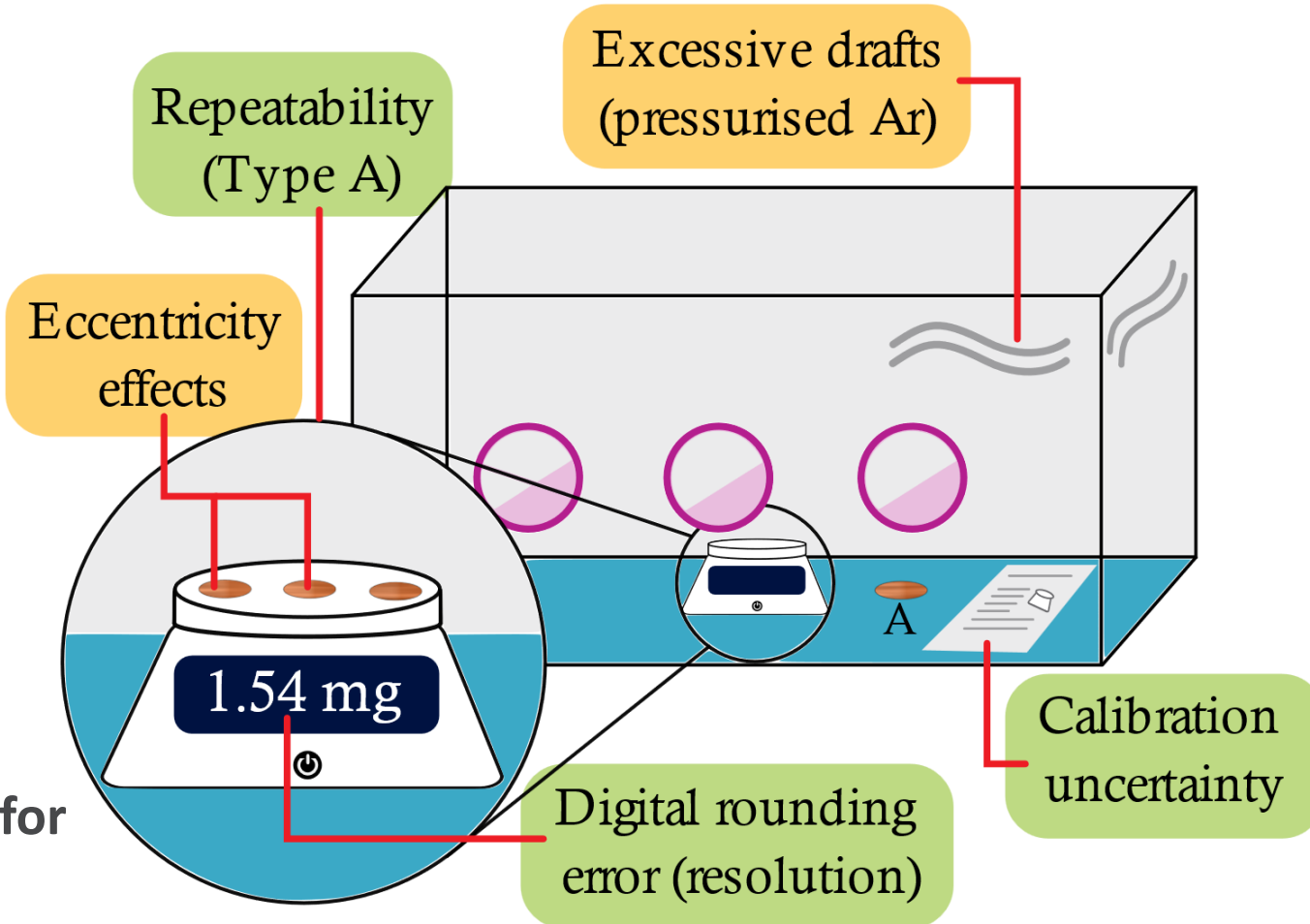


3. TEARDOWN PROCESS



4. SOURCES OF UNCERTAINTY

This diagram shows the **sources of uncertainty** in the mass measurement.



- = accounted for in budget
- = assumed resolved during calibration

Uncertainty analysis **assumes perfect operation²** (impossible!) but can be reduced by methodology improvement such as **regular calibration** or using a **concrete table** to minimise vibrations.

5. MONTE CARLO METHOD

The **standard (not expanded) uncertainty** of mass loading and thickness found in the gravimetric budget was set to be the **standard deviation** of the input values.

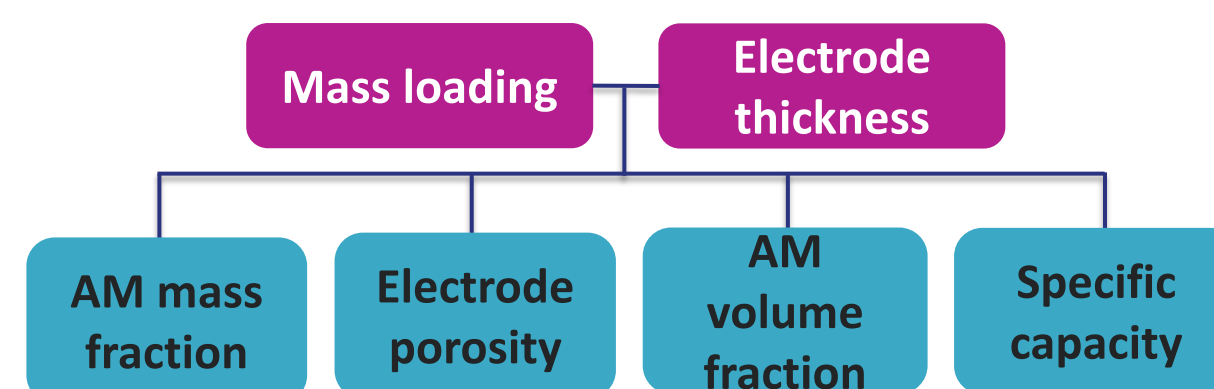
Defining the measurand X_i
A **normally distributed array** of values was generated from the mean and deviation found in the budget and using a **quasi-random sequence**.

Perform the calculations N times
Iterate calculations over array values using **for-loops**.

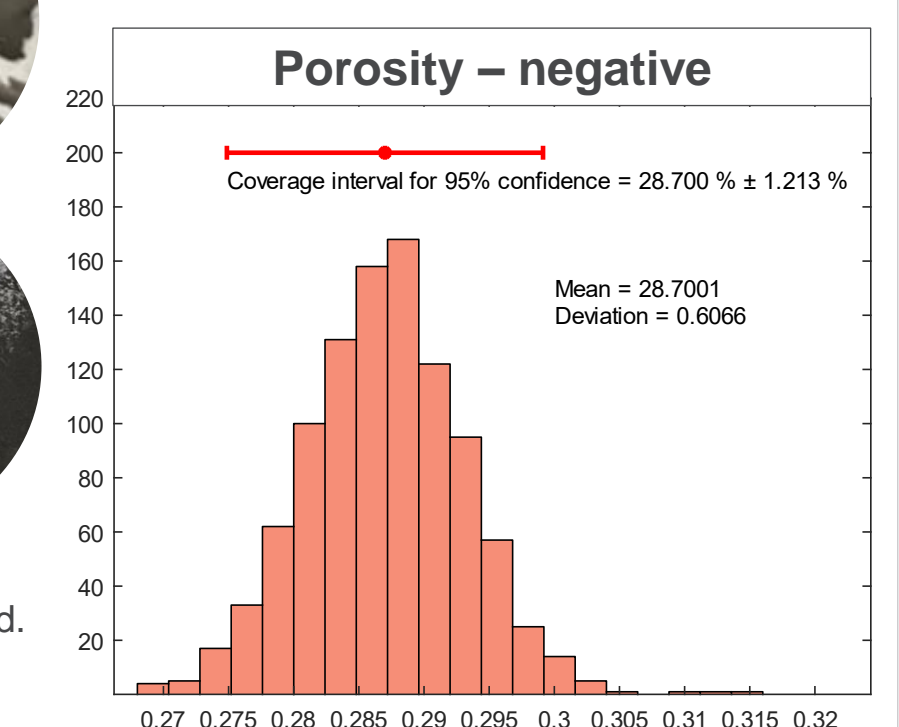
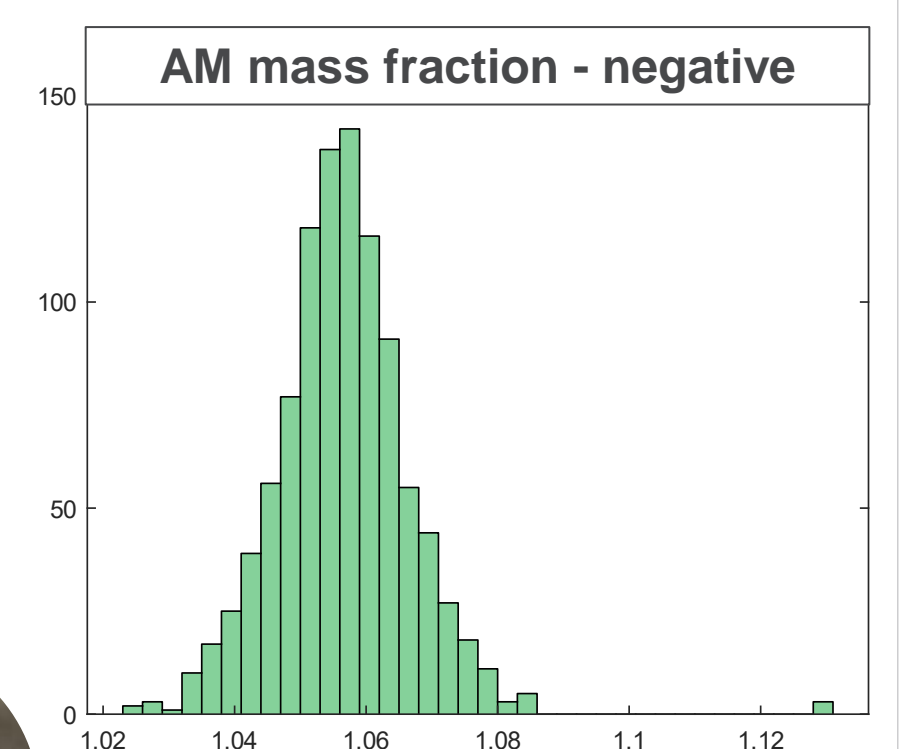
Obtain output Y_i
Fit a normal distribution to Y_i histogram to find deviation.

7. CONCLUSIONS

- Between thickness and mass loading of active material (AM), **mass loading was the dominant** uncertainty.



- An uncertainty of 10% in the mass loading resulted in an uncertainty of **38%** in the porosity:
- The uncertainty in the negative electrode parameters was generally greater due to **(A) some active material sticking to the separator** and **(B) active material flaking off as a powder** and hence, being lost.



- Uncertainty tool embedded in spreadsheet:

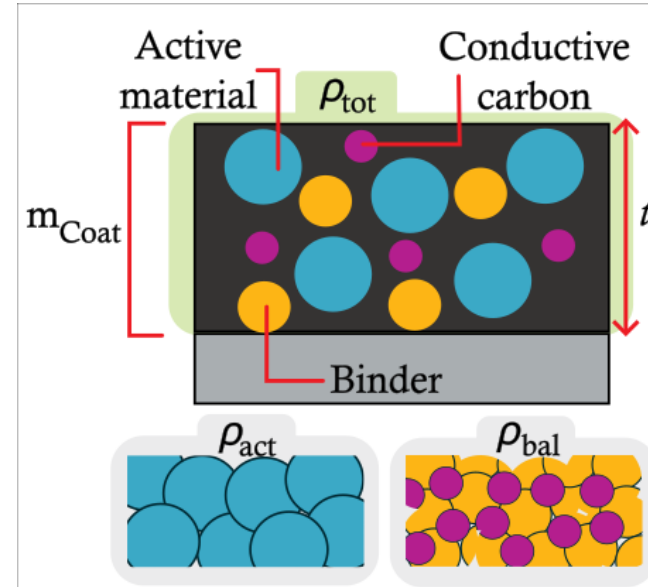
Sample coated on a single side	Diameter / cm	Mass / mg	Thickness / μm	Coat thickness / μm	Coat mass / mg	Mass loading / mg cm^{-2}
Average	1.8	52.420	9.25E+01	84.490	34.28	13.471
Uncertainty 95% confidence	5.40E-03	0.117	3.51E-03	0.005	1.48E-01	0.082

6. EQUATIONS

The equation for **porosity, ϵ** , is shown on the right. **m_{Coat} is the mass loading** of the electrode layer. **ρ_{tot} is the electrode density** which is calculated from the **active material mass fraction, w_{act}** .

$$\epsilon = \frac{1 - m_{\text{Coat}}}{1000 \times t \times \rho_{\text{tot}}}$$

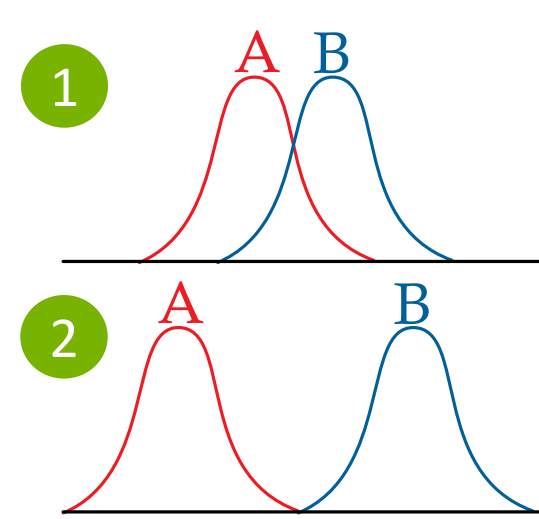
$$\frac{1}{\rho_{\text{tot}}} = \frac{w_{\text{act}}}{\rho_{\text{act}}} + \frac{1 - w_{\text{act}}}{\rho_{\text{bal}}}$$



w_{act} depends on capacity which is inversely proportional to mass loading. Hence, **porosity is a complex function of mass loading**, and would be tricky to solve analytically.

8. IMPACT / NEXT STEPS

- In both figures the mean of B is greater than the mean of A. However, the **conclusion that $B > A$ cannot be drawn** for (1) due to **significant overlap**.
- Hence, uncertainty analysis enables **quantitative comparison** between measurements under **different conditions**.



Future steps:

- Improve equipment + setup
- Electrochemical measurement uncertainties
- Uncertainty in supply chain

REFERENCES

- (1) Bell, S. (2001) 'A Beginner's Guide to Uncertainty of Measurement', Measurement Good Practice Guide No. 11 (Issue 2), Teddington: National Physical Laboratory.
- (2) Davidson, S., Perkin, M., Buckley, M. (2004) 'The Measurement of Mass and Weight', Measurement Good Practice Guide No. 71, Teddington: National Physical Laboratory.

INTERN BIO

Siddhi is a 3rd year Materials Science student at the University of Cambridge. She hopes to pursue a PhD in the battery sector and transition to industry to make a positive, sustainable impact! She would love to establish a start-up in the future within the energy storage industry.

